Recharge Guide

Everything you need to know about Recharge...and then some

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The purpose of this guide is to teach you everything you need to know about recharge. I have broken up this guide into chapters in an effort build up your understanding on how recharge works. My methods for building up your knowledge will be a bit backwards. Normally in a textbook, you will be given a formula, the formula will be derived, then you will see examples on how to use the formula. Instead, Chapter 1 will show you examples with step-by-step solutions in hopes of learning and observing all the details that goes into solving the Recharge Problem. In Chapter 2, I will introduce formulas that could be used for solving the examples from Chapter 1 in hopes that you can apply those formulas for your own needs. In Chapter 3, I introduce a new technique for solving the Recharge Problem that is faster and easier to implement, although it has its limitations. At that point, you will have all the knowledge you need to know. But if you would like to read on, Chapter 4 provides additional formulas that apply to the Recharge Problem that could be useful to you. Finally, Chapter 5 (not complete), will be additional examples that I will solve by request. If you have a specific problem and are having trouble, you can mention it in the comments and I will attempt to solve it and provide the solution in this chapter.

Chapter 1: Understanding How to Calculate the Time to Recharge a Power

The first thing to understand about recharge is that we are working with two time domains: the real-world time domain (which is what you experience), and the cooldown time domain (which is what your power experiences). The recharge in the power is the rate at which the cooldown time domain experiences for every second that passes in the real-world time domain. This leads us to our first formula, which is the amount of cooldown time experienced.

 $Time_{CD} = Recharge \times Time_{Real}$

To understand how to apply this formula, let's start with the most common example recharge question: How much recharge do I need to make Hasten permanent?

Example #1.1: Hasten has a base recharge of 450 seconds and a duration of 120 seconds. Thus, to make Hasten permanent, we need our power to experience 450s of cooldown within 120s of real-world time. To know the amount of recharge required to achieve that, we use algebra to tweak our above formula:

$$Recharge = \frac{Time_{CD}}{Time_{Real}} = \frac{450}{120} = 3.75 = 375\%$$

375% recharge may seem like a lot, however 100% comes from our base recharge and another 70% comes from Hasten, so that leaves us with needing an additional 205% recharge from other sources (enhancements, set IO bonuses, other powers).

Example #1.2: Now let's say we only have 370% recharge (70% from Hasten, 300% from base and other sources). How long will it take for Hasten to recharge?

This requires us to analyze the problem in two parts. First part, we analyze when Hasten is active (370% recharge for 120 seconds) and the second part we analyze when Hasten wears off (300% recharge for some additional amount of time). Our power will still need to experience 450s of cooldown, so:

$$Time_{CD} = Recharge_{Hasten} \times (HastenDuration) + Recharge_{NoHasten} \times Time_{Add}$$
$$450 = (3.00 + 0.70) \times 120 + 3.00 \times Time_{Add}$$
$$Time_{Add} = \frac{450 - 3.70 \times 120}{3.00} = \frac{6}{3.00} = 2$$

This tells us Hasten will recharge in 120 + 2 = 122 seconds.

Example #1.3: Now let's do the same example, but this time a Force Feedback Proc (+100% recharge for 5 seconds) goes off once while Hasten is active. How long would it take for Hasten to recharge?

This adds some additional complexity as we don't know if Hasten will become permanent or not, so we may have to analyze this in up to three parts: Hasten+FF active (for 5 seconds), Hasten active (120 seconds minus the 5 secs for FF proc), and nothing active (for possibly some additional amount of time). To make this simple, we will start from highest recharge then work our way down to calculate the amount of cooldown experienced for each time interval of differing recharge values:

$$Time_{CD} = 450 = (3.00 + 0.70 + 1.00) \times 5 + (3.00 + 0.70) \times (120 - 5) + 3.00 \times Time_{Add}$$
$$450 = 23.5 + 425.5 + 3 \times Time_{Add}$$
$$Time_{Add} = \frac{450 - 425.5 - 23.5}{3.00} = 1/3$$

It turns out we still do not achieve permanent Hasten as it would take 120 + 0.33 = 120.33 seconds to recharge. If *Time_{Add}* was equal to or less than zero, then we would have achieved permanent Hasten as this would tell us we achieved full recharge prior to 120 seconds.

Example #1.4: Now let's assume we had two Force Feedback Procs occur (a total of 10 seconds worth of +100% recharge boost). What would become the final recharge for Hasten?

We do the same steps as above.

$$Time_{CD} = 450 = 4.70 \times (5+5) + 3.70 \times (120 - 5 - 5) + 3.00 \times Time_{Add}$$
$$Time_{Add} = \frac{450 - 47 - 407}{3.00} = -1.33$$

Now we have a negative number in the additional time calculation. This tells us that Hasten actually finished recharging prior to the expiration of Hasten's 120 second duration (yay, we achieved perma-Hasten). However, how long did it actually take to recharge? We need to tweak the numbers in the above formula by removing the 120 seconds from the Hasten duration, as we know we will never reach that time, and substitute it with our $Time_{Add}$:

$$Time_{CD} = 450 = 4.70 \times 10 + 3.70 \times (Time_{Add})$$
$$Time_{Add} = \frac{450 - 47}{3.70} = 108.92$$

It turns out that the total time for Hasten to recharge in this example is 10 + 108.92 = 118.92 seconds.

Let's do a few more examples by incorporating a Tier 4 Ageless Destiny incarnate power (Core Epiphany or Radial Epiphany). This power has a 120 second cooldown duration that is unaffected by recharge; and when it is cast, it will provide a recharge bonus that cascades from strongest boost to weakest boost. It provides a 70% recharge boost for the first 10 seconds, then 30% for the next 20 seconds, then 20% for the next 30 seconds, then 10% for the final 60 seconds (120 seconds in total).

Example #1.5: Let's assume once again that we have 300% recharge in the Hasten power from outside sources. How long will it take for Hasten to recharge if we cast Ageless and Hasten back-to-back?

Once again, we break this down by time intervals of where the recharge in Hasten is different.

$$Time_{CD} = 450$$

$$= (3.00 + 0.70 + 0.70) \times 10 + (3.00 + 0.30 + 0.70) \times 20$$

$$+ (3.00 + 0.20 + 0.70) \times 30 + (3.00 + 0.10 + 0.70) \times Time_{Add}$$

$$450 = 44 + 80 + 117 + 3.80 \times Time_{Add}$$

$$Time_{Add} = \frac{450 - 44 - 80 - 117}{3.80} = \frac{209}{3.80} = 55$$

This tells us Hasten will recharge in 10 + 20 + 30 + 55 = 115 seconds, thus achieving perma-Hasten.

Example #1.6a: Finally, let's look at incorporating the Force Feedback Proc into this Ageless example. Now we care about when the Force Feedback Proc fires because if it fires within the first 10 seconds, then we will achieve a total recharge of 300%+70%+70%+100% = 540% which is over the maximum allowed recharge cap of 500%. So, let's look at the impact of Hasten's recharge if the FF Proc fires in the first 10 seconds and if it fires after 10 seconds.

For first 10 seconds we get the following recharge-capped result

$$Time_{CD} = 450 = 5.00 \times 5 + 4.40 \times (10 - 5) + 4.00 \times 20 + 3.90 \times 30 + 3.80 \times Time_{Add}$$
$$Time_{Add} = \frac{450 - 25 - 22 - 80 - 117}{3.80} = \frac{206}{3.80} = 54.2105$$

Thus, Hasten would recharge in 60 + 54.2105 = 114.2105 seconds.

Example #1.6b: Now let's look at FF Proc firing after 10 seconds (thus, never surpassing recharge cap). It won't matter where it fires as the math will not change the result, so let's assume it happens in the subsequent 20 second window.

$$Time_{CD} = 450$$

= 4.40 × 10 + (4.00 + 1.00) × 5 + (4.00) × (20 - 5) + 3.90 × 30
+ 3.80 × Time_{Add}
$$Time_{Add} = \frac{450 - 44 - 25 - 60 - 117}{3.80} = \frac{204}{3.80} = 53.6842$$

Thus, Hasten recharges in 60 + 53.6842 = 113.6842 seconds, which is slightly faster than the recharge capped scenario as we don't waste any of our boosts.

Chapter 2: Formulas for Calculating a Power's Recharge Time

by using Time Interval Analysis

I know that was a lot of math and a lot of examples I just threw at you. I didn't do that for the purpose of triggering your math class PTSD, I did it because it is my goal to make you an expert in understanding how recharge works and how to calculate a power's recharge for ANY situation. These examples covered everything ranging from static recharge, fluctuating recharge, and capsaturated recharge; so, if you were able to follow the math in those examples, you will have an easier time following the formulas I'm about to introduce. All these formulas were used in the examples, but now I will call them out explicitly.

Recall our first formula,

Formula 2.1:

$Time_{CD} = Recharge \times Time_{Real}$

We tweaked this first formula by accommodating for times when the recharge changes:

$$Time_{CD} = Rch_1 \times Time_{R1} + Rch_2 \times Time_{R2} + \dots + Rch_N \times Time_{RN} = \sum_{n=1}^{N} (Rch_n \times Time_{Rn})$$

This simply shows that we are calculating the total cooldown time by summing the products of each (n-th) recharge amount with its respective real-world time duration. We used this formula in almost every example by plugging in the Base Recharge of the power as our $Time_{CD}$, then adding up the total recharge amount for each known time interval and multiplying them together, then solving for the last unknown time interval (where $Time_{Add}$ is the $Time_{RN}$ in this formula). To show this explicitly, let's recall Example #1.3 and apply it to Formula 2.2.

$$Time_{CD} = 450 = (3.00 + 0.70 + 1.00) \times 5 + (3.00 + 0.70) \times (120 - 5) + 3.00 \times Time_{Add}$$
$$Time_{CD} = BaseRecharge = Rch_1 \times Time_{R1} + Rch_2 \times Time_{R2} + Rch_3 \times Time_{R3}$$

We have the following:

$$BaseRecharge = 450 \ seconds$$

$$Rch_1 = 3.00 + 0.70 + 1.00 = 4.70$$

$$Time_{R1} = 5 \ seconds$$

$$Rch_2 = 3.00 + 0.70 = 3.70$$

$$Time_{R2} = 120 - 5 = 115 \ seconds$$

$$Rch_3 = 3.00$$

$$Time_{R3} = Time_{Add}$$

We can rearrange the above formula to solve for $Time_{Add}$ directly.

Formula 2.3:

$$Time_{Add} = \left(BaseRecharge - \sum_{n=1}^{N-1} (Rch_n \times Time_{Rn})\right) / Rch_N$$

From this, we can calculate the total time it takes for a power to recharge by simply adding up all the time intervals together. This formula can go without saying, but I provide it for completeness.

Formula 2.4:

$$Time_{Recharge} = Time_{R1} + Time_{R2} + \dots + Time_{RN-1} + Time_{Add} = \sum_{n=1}^{N-1} Time_{Rn} + Time_{Add}$$

Finally, the total recharge of the power for each time interval is simply the summation of each source of recharge that is present for the entirety of its time interval.

Formula 2.5:

$$Rch_n = \min(P_{Total} + T_{Total}, 500\%) = \min\left(\sum_{l=1}^{L} P_l + \sum_{m=1}^{M} T_m, 500\%\right)$$

Where we add up all permanent recharge boosts (P_l , which represents the l-th permanent boost out of a total of L permanent boosts) and we add up all temporary boosts (T_m , which represents the m-th temporary boost out of a total of M temporary boosts) that are active for the entirety of the n-th time interval. If the total recharge boosts exceed 500%, then it is capped to 500%.

That's admittedly a confusing statement and a confusing formula for something so simple. I'm sorry. So, let me put this in layman's terms... the total recharge is calculated by adding up all the recharge sources for the power. You know how to do this, as I showed how to do it in each of the examples. Permanent boosts include your 100% base recharge, the power's recharge enhancements (after enhancement diversification), global set IO bonuses (e.g. slotting a Luck of the Gambler: Defense/Increased Recharge Speed, or 5-slotting an Apocalypse set), or possibly auto powers (e.g. Quickness, or Lightning Reflexes). Temporary boosts include powers with a finite duration (e.g. Hasten, Ageless Destiny) and temporary buffs (e.g. Force Feedback Proc). Recall from Example #6a:

$$Time_{CD} = 450 = 5.00 \times 5 + 4.40 \times (10 - 5) + 4.00 \times 20 + 3.90 \times 30 + 3.80 \times Time_{Add}$$

What we had in this example was the following:

$$\begin{aligned} Rch_1 &= \min\left(\frac{P_1 + \dots + P_L}{300\%} + \frac{T_1}{70\%} + \frac{T_2}{70\%} + \frac{T_3}{100\%}, 500\%\right) = \min(540\%, 500\%) = 5.00\\ Rch_2 &= \min\left(\frac{P_1 + \dots + P_L}{300\%} + \frac{T_1}{70\%} + \frac{T_2}{70\%}, 500\%\right) = \min(440\%, 500\%) = 4.40\\ Rch_3 &= \min\left(\frac{P_1 + \dots + P_L}{300\%} + \frac{T_1}{30\%} + \frac{T_2}{70\%}, 500\%\right) = \min(400\%, 500\%) = 4.00\\ Rch_4 &= \min\left(\frac{P_1 + \dots + P_L}{300\%} + \frac{T_1}{20\%} + \frac{T_2}{70\%}, 500\%\right) = \min(390\%, 500\%) = 3.90\\ Rch_5 &= \min\left(\frac{P_1 + \dots + P_L}{300\%} + \frac{T_1}{10\%} + \frac{T_2}{70\%}, 500\%\right) = \min(380\%, 500\%) = 3.80 \end{aligned}$$

In this example, Rch_1 had its summation of boosts exceed the 500% cap, so the min-function capped the total boost to 500%. All the other Rch values did not exceed the cap.

Also, in this example, I had spelled out what all the temporary boosts were, so I was able to break them out here by their T_1 , T_2 , etc. As for the 300% permanent boosts coming from other sources, I never did say where all those boosts came from. In actuality, we know our base is $P_1 = 100\%$. Then we may have enhancements that make of $P_2 = 95\%$. We might have 4 Luck of the Gamblers in our build giving us $P_3 = P_4 = P_5 = P_6 = 7.5\%$. We might have global set IO bonuses that give us a total of $P_7 = 55\%$. Finally, we might have an auto power such as Quickness that gives us $P_8 = 20\%$. Thus, we achieve a total permanent recharge boost of

$$P_{Total} = \sum_{l=1}^{8} P_l = P_1 + P_2 + P_3 + P_4 + P_5 + P_6 + P_7 + P_8$$

= 100\% + 95\% + 7.5\% + 7.5\% + 7.5\% + 7.5\% + 55\% + 20\% = 300\%

Overall, this is overkill for understanding how to calculate the total permanent recharge in a power. Honestly, you only need to check 2 things and you can do this in the game or in Mids' Reborn: Look up the amount of recharge slotted in the power (the Enhancement Diversification amount), and look up your Global Recharge **when no temporary boosts are active** (so turn off Hasten and similar powers). If using Mids' Reborn, you will see this as "+Recharge" in the Totals tab, or as "Haste" in the View Totals/Misc. Buffs panel. Once you have those 2 numbers, add them together with your base recharge and you will get your P_{Total}

$$P_{Total} = P_{Base} + P_{Enhanced} + P_{Global}$$

Chapter 3: Formulas for Calculating a Power's Recharge Time

using Recharge Boost Duration Analysis

In Chapter 1, I used step-by-step examples to show how we can calculate the time it takes for a power to fully recharge by breaking up the analysis into time intervals where the total recharge in each time interval is constant. In Chapter 2, I showed the formulas we would use to do the type of analysis performed in those examples. Now I want to change course by breaking up the analysis by recharge boost as opposed to breaking up the analysis by time intervals. Below I use graphs to illustrate what I mean by this:



Figure 3.1: Time Interval Analysis

Figure 3.1 is the same as the analysis we did in Example #1.3, instead the total permanent boost was 300% in Example #1.3 whereas this figure shows it as 250%. Nonetheless, it illustrates how we analyzed the problem: For the first 5 seconds we calculated the cooldown time for when the Force Feedback Proc and Hasten were active at the same time (white), then the next 115 seconds was evaluated for when only Hasten was active (yellow), then an additional amount of time was evaluated for when only the permanent boosts were active (green). That additional amount of time was what we solved for.



Figure 3.2: Recharge Boost Duration Analysis

In Figure 3.2, we highlight how we can instead analyze for each individual recharge boost and its duration. The temporary boosts are evaluated for just amount and duration, while the permanent

boosts are evaluated until the time the power becomes fully recharged (which is what we'll solve for).

The benefit of this method is that it is time agnostic. We don't need to worry about calculating time intervals for when each recharge boost is active/inactive, which makes for easier and faster calculations. The downside of this method, by ignoring when boosts are active (thus not knowing how much recharge is stacked up) we could go over the 500% recharge cap, resulting in inaccurate calculations. So, keep this in mind when considering using the following formulas as **they will only be accurate if your boosts never go over the 500% recharge cap**. Lucky for most of us, this will typically be the case...and even if we were to temporarily go over the recharge cap, it likely won't be sustained long enough to change our final results by a whole lot (Examples #1.6a and #1.6b in Chapter 1 shows this).

Once again, recall our first formula

$Time_{CD} = Recharge \times Time_{Real}$

In Chapters 1 and 2, we used this principal formula to add up all the cooldown times from different time intervals and its respective total recharge amounts. By adding up all the cooldown times by recharge boost amounts with its respective boost durations does not change this math at all. We are just calculating area with different lengths and widths, essentially, but we will come to the same end result.

Formula 3.1:

$$Time_{CD} = BaseRecharge = \sum_{m=1}^{M} (T_m \times Dur_m) + \sum_{l=1}^{L} (P_l \times Time_{Recharge})$$

Recall from Chapter 2, the T_m is the amount of the m-th temporary recharge boost and P_l is the amount of the l-th permanent recharge boost. For each of the temporary recharge boosts it has a duration which is represented as Dur_m . For all permanent recharge boosts, they are evaluated until the power is recharged. Note: there is one caveat I should make to Formula 3.1, which is each duration of a temporary boost can't be greater than the recharge time (similar to Example #1.4). If that is the case, then we must treat the temporary boost as a permanent boost and only evaluate it for the time until the power recharges.

Formula 3.1a:

$$BaseRecharge = \sum_{m=1}^{M} (T_m \times \min(Dur_m, Time_{Recharge})) + \sum_{l=1}^{L} (P_l \times Time_{Recharge})$$

Since we are solving for $Time_{Recharge}$, we unfortunately won't know if the duration of a temporary recharge boost will be greater (perma'd) until we run the numbers. So, like the Example #1.4, if we find our solution to be in error, i.e. $Time_{Recharge} < any(Dur_m)$, then we must iterate through our analysis by changing the longest temporary boost duration to $Time_{Recharge}$,

recalculate, then check the remaining temporary boost durations to see if any of those are still in error.

That sounds like a painful process, and it certainly can be, but you can save yourself some of the hassle if you know ahead of time which temporary recharge boosts will definitely be active for the entirety of your power's recharge and treat those boosts as permanent right away (turn a T_m into a P_l , basically). This could be done by identifying temporary powers that are already perma'd (if we know Hasten or ChronoShift are already perma'd, then treat them as permanent), or it could be your power has a base recharge less than the duration of a temporary boost. By handling those situations ahead of time, you can save yourself from a lot of the potential iterations you might need.

Let's not dwell on Formula 3.1a. I will show how it works in a later example, but for now let's use Formula 3.1 to define some other useful functions.

Since each permanent boost is being multiplied by the same time duration ($Time_{Recharge}$), we can actually add up all the permanent boosts together first, then multiply. This tweaks our formula slightly:

Formula 3.1b:

$$BaseRecharge = \sum_{m=1}^{M} (T_m \times Dur_m) + \sum_{l=1}^{L} (P_l \times Time_{Recharge})$$
$$= \sum_{m=1}^{M} (T_m \times Dur_m) + Time_{Recharge} \times \sum_{l=1}^{L} (P_l)$$
$$= \sum_{m=1}^{M} (T_m \times Dur_m) + Time_{Recharge} \times P_{Total}$$

This now makes it simple to solve for the time it takes a power to recharge.

Formula 3.2:

$$Time_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total}}$$

This is as simple as it comes with solving for a power's recharge time. We merely take the base recharge of the power, subtract the product of each temporary recharge boost and its duration, then divide by the total permanent recharge boost.

Let's revisit some of the examples we did before, now using the Formula 3.2.

Example #3.1: Recall in Example #1.3, we had a $P_{Total} = 300\%$, and a single Force Feedback Proc. How long would it take for Hasten to recharge?

$$Time_{Recharge} = \frac{450 - (1.00) \times 5 - (0.70) \times 120}{3.00} = \frac{450 - 5 - 84}{3.00} = \frac{361}{3.00} = 120.33$$

Same answer as before.

Now let's look at an Ageless Destiny example. If you recall from before, I said Ageless works as a 70% recharge for 10 seconds, then 30% for the next 20 seconds, 20% for the next 30 seconds, then 10% for the final 60 seconds. If you read the description of Ageless, that is not what it says. It actually says it provides a 40% recharge boost for 10 seconds, a 10% recharge boost for 30 seconds, a 10% recharge boost for 60 seconds, and a 10% recharge boost for 120 seconds. My original description simply added the stacks of recharge together, here we will use the actual description as four separate recharge boosts.

Example #3.2: Recall from Example #1.5, we have a $P_{Total} = 300\%$ and we cast Ageless and Hasten back-to-back. How long will it take for Hasten to recharge?

$$Time_{Recharge} = \frac{450 - 0.40 \times 10 - 0.10 \times 30 - 0.10 \times 60 - 0.10 \times 120 - 0.70 \times 120}{\frac{3.00}{3.00}} = \frac{3.00}{\frac{3.41}{3.00}} = 113.67$$

Oops, we have a $Time_{Recharge}$ that is less than the duration of two of our temporary boosts (see Formula 3.1a). Since both boosts have a 120 second duration and we now know the recharge is less than 120 seconds, we must re-do our calculation with these temporary boosts treated as permanent boosts.

$$Time_{Recharge} = \frac{450 - 0.40 \times 10 - 0.10 \times 30 - 0.10 \times 60}{3.00 + 0.10 + 0.70} = \frac{437}{3.80} = 115$$

Once again, this is the same answer as before.

From these examples we can see that using Recharge Boost Duration analysis is viable, if not ultimately more convenient. The nice thing with this method is that you can see a temporary boost and instantly know what its impact on a power will be. For example, the Force Feedback Proc's 5 seconds of 100% recharge effectively takes off 5 seconds of a power's base recharge. Hasten's 120 seconds of 70% recharge effectively takes off 84 seconds. Those are numbers you can quickly calculate and apply whenever you need.

Chapter 4: Additional Useful Formulas

So far, I've taken you through an exhaustive journey in understanding how to do one calculation: Time to Recharge. Now I want to go through some of the formulas you can use to answer some of the more common questions that come up relating to recharge. For this chapter, I will format it more like a FAQ section.

How much will an extra 10% recharge give me?

Answer: Ok, this can be any percentage really, so we will just say an "extra X recharge", where X is in decimal form (like the decimals I've been using in my examples). Anyways, this is pretty simple to apply.

Formula 4.1:

$$New_{Recharge} = Old_{Recharge} \times \left(\frac{P_{Total}}{P_{Total} + X}\right)$$

Proof (using Formula 3.2):

$$Old_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total}}$$
$$New_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total} + X}$$
$$New_{Recharge} \times (P_{Total} + X) = Old_{Recharge} \times P_{Total}$$

Pretty simple. You actually don't even need to know your base recharge or the temporary boosts in the power. As long as you know what your current ("old") recharge is, and you know your total permanent boosts (including any temporary boosts that are active the entire duration, Formula 3.1a), then you can directly calculate the effects of adding more recharge simply by using Formula 4.1. There is one potential gotcha, though. If your added recharge would turn a previously temporary boost into an effective permanent boost, then you're out of luck. You'll have to go ahead an incorporate the base recharge and temporary boosts and calculate the new recharge directly as shown in the above proof.

Example #4.1: Let's assume our power is Hasten with a $P_{Total} = 250\%$. We assume we have one Force Feedback Proc occur. We calculate our recharge to be:

$$Time_{Recharge} = \frac{450 - 0.70 \times 120 - 1.00 \times 5}{2.50} = 144.4 \, sec$$

We want to know what our new recharge time would be if we added a 10% global recharge boost via 5-slotting a purple IO set.

Answer:

$$New_{Recharge} = (144.4) \times \left(\frac{2.50}{2.50 + 0.10}\right) = 138.85 \ sec$$

How much will a Force Feedback Proc give me?

Answer: Again, this can be any temporary recharge boost for any duration. So, we'll assume the amount of boost is Y (Y = 1.00 for FF proc) and the duration is $Dur_Y (Dur_Y = 5 \text{ for FF proc})$.

Formula 4.2:

$$New_{Recharge} = Old_{Recharge} - \frac{Y \times Dur_Y}{P_{Total}}$$

Proof (from Formula 3.2):

$$Old_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total}}$$

$$New_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m) - Y \times Dur_Y}{P_{Total}}$$

$$New_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total}} - \frac{Y \times Dur_Y}{P_{Total}}$$

Once again, this is a very simple formula as you only need to know your current ("old") recharge and your total permanent recharge boosts. However, once again, if the new boost winds up making a temporary boost effectively a permanent boost, then you will have to calculate the new recharge directly as shown in this proof and properly applying the Formula 3.1a caveat.

Example #4.2: Let's use the result from Example #4.1, but now let's assume we get one additional Force Feedback Proc to occur. What is our new recharge for Hasten?

Answer:

$$New_{Recharge} = 138.85 - \frac{1.00 \times 5}{2.60} = 136.92 \, sec$$

How much equivalent recharge does a Force Feedback Proc provide me?

Answer: Often I've seen the question come up of how helpful is a temporary recharge boost, compared to simply adding more global (permanent) recharge. Often you might see someone respond to this question with something like "a single Force Feedback Proc is equivalent to adding 6% global recharge". Now, that response is not universal; it is specific only to power in question and the build it is applied to. But wouldn't you like to know how people come up with those types of responses? Well, there's a formula for that too…

Formula 4.3:

$$X = \left(\frac{Old_{Recharge}}{Y \times Dur_{Y}} - \frac{1}{P_{Total}}\right)^{-1}$$

Proof (from Formula 3.2):

$$New_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total} + X} \\ = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m) - Y \times Dur_M}{P_{Total}}$$

$$P_{Total} \times \left(BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)\right)$$

= $(P_{Total} + X) \times \left(BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m) - Y \times Dur_Y\right)$
$$0 = X \times \left(BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m) - Y \times Dur_Y\right) - P_{Total} \times Y \times Dur_Y$$

$$X = \frac{P_{Total} \times Y \times Dur_Y}{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m) - Y \times Dur_Y}$$

$$X = \frac{P_{Total} \times Y \times Dur_Y}{Old_{Recharge} \times P_{Total} - Y \times Dur_Y}$$

$$X = \frac{1}{\frac{Old_{Recharge}}{Y \times Dur_Y} - \frac{1}{P_{Total}}}$$

The proof is probably uglier than doing the actual brute force calculations themselves. In fact, once you calculate your new recharge from the temporary buff, you should simply solve directly:

Formula 4.3a:

$$X = P_{Total} \times \left(\frac{Old_{Recharge}}{New_{Recharge}} - 1\right)$$

Proof (from Formula 3.2):

$$New_{Recharge} = \frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m) - Y \times Dur_Y}{P_{Total}}$$

$$\frac{BaseRecharge - \sum_{m=1}^{M} (T_m \times Dur_m)}{P_{Total} + X} = New_{Recharge}$$

$$\frac{Old_{Recharge} \times P_{Total}}{P_{Total} + X} = New_{Recharge}$$

$$X = \frac{Old_{Recharge} \times P_{Total}}{New_{Recharge}} - P_{Total}$$

Example #4.3: Let's reuse the results of Example #4.2. In it we had one additional Force Feedback Proc occur, which changed the recharge of Hasten from 138.85 seconds to 136.92 seconds. What amount of additional recharge would be required to replicate that one additional Force Feedback Proc?

Answer: Using Formula 4.3 we get:

$$X = \left(\frac{Old_{Recharge}}{Y \times Dur_{Y}} - \frac{1}{P_{Total}}\right)^{-1} = \left(\frac{138.85}{1.00 \times 5} - \frac{1}{2.60}\right)^{-1} = 0.036517 \ (3.65\%)$$

Using Formula 4.3a we get:

$$X = \frac{Old_{Recharge} \times P_{Total}}{New_{Recharge}} - P_{Total} = \frac{138.85 \times 2.60}{136.92} - 2.60 = 0.036517 (3.65\%)$$

Now let's check our work. If we had added 3.65% recharge instead of the one additional Force Feedback Proc, would we get the same new recharge?

$$New_{Recharge} = Old_{Recharge} \times \left(\frac{P_{Total}}{P_{Total} + X}\right) = 138.85 \times \left(\frac{2.60}{2.60 + 0.036517}\right) = 136.92$$

Indeed, in this specific example, the additional Force Feedback Proc provided the equivalence of 3.65% global recharge to Hasten. But if you used different numbers (different P_{Total} , $Old_{Recharge}$, etc), you would certainly get different results.